

**Nonlinear polymer rheology:**  
Macroscopic phenomenology and molecular foundation

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PREFACE

INTRODUCTION

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